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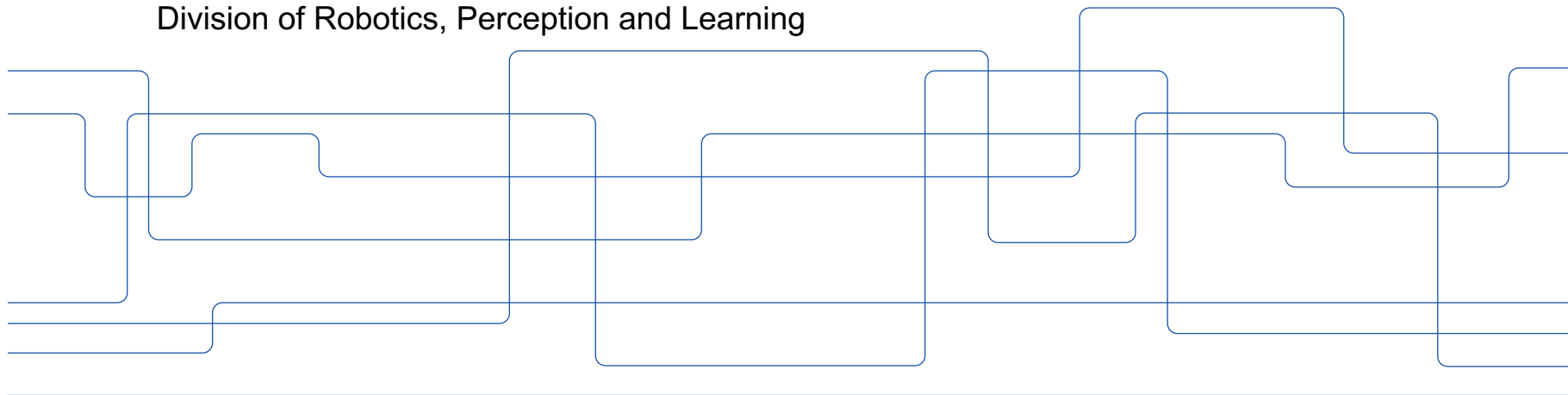
KTH ROYAL INSTITUTE  
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# Formal methods for robot planning

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## Why formal methods?

Rigorous techniques for  
specification



How do we tell  
robots what to do?

development,  
verification,  
analysis of systems



How do we ensure  
that they behave  
as expected?



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## Why temporal logics and formal synthesis?

Temporal logics

- rich
- rigorous
- resemblance to natural language



How do we tell robots what to do?

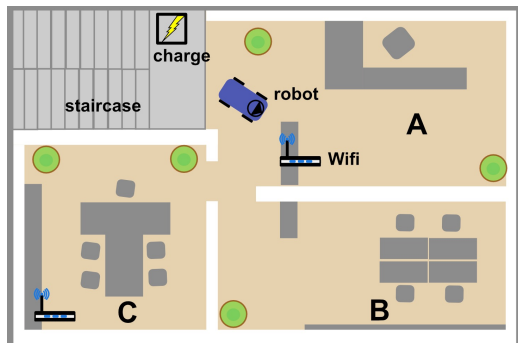
Formal synthesis



How do we ensure that they behave as expected?



## Temporal logic for mission and motion objectives



- Keep patrolling the three offices.

$$GF(A) \wedge GF(B) \wedge GF(C)$$

- Whenever you spot danger, go directly to the staircase and wait for “all clear” signal before continuing.

$$G(\text{danger} \Rightarrow X(\text{staircase} \ U \ \text{all\_clear}))$$

- Make sure to recharge at least every 10 minutes.

$$GF_{[0,10]} \text{recharge}$$

- At all times, stay within 5 meters from the wi-fi router.

$$G(\text{Dist}(\text{robot}, \text{router}) \leq 5)$$



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## Why temporal logics and formal synthesis?

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How do we tell robots what to do?

Formal synthesis

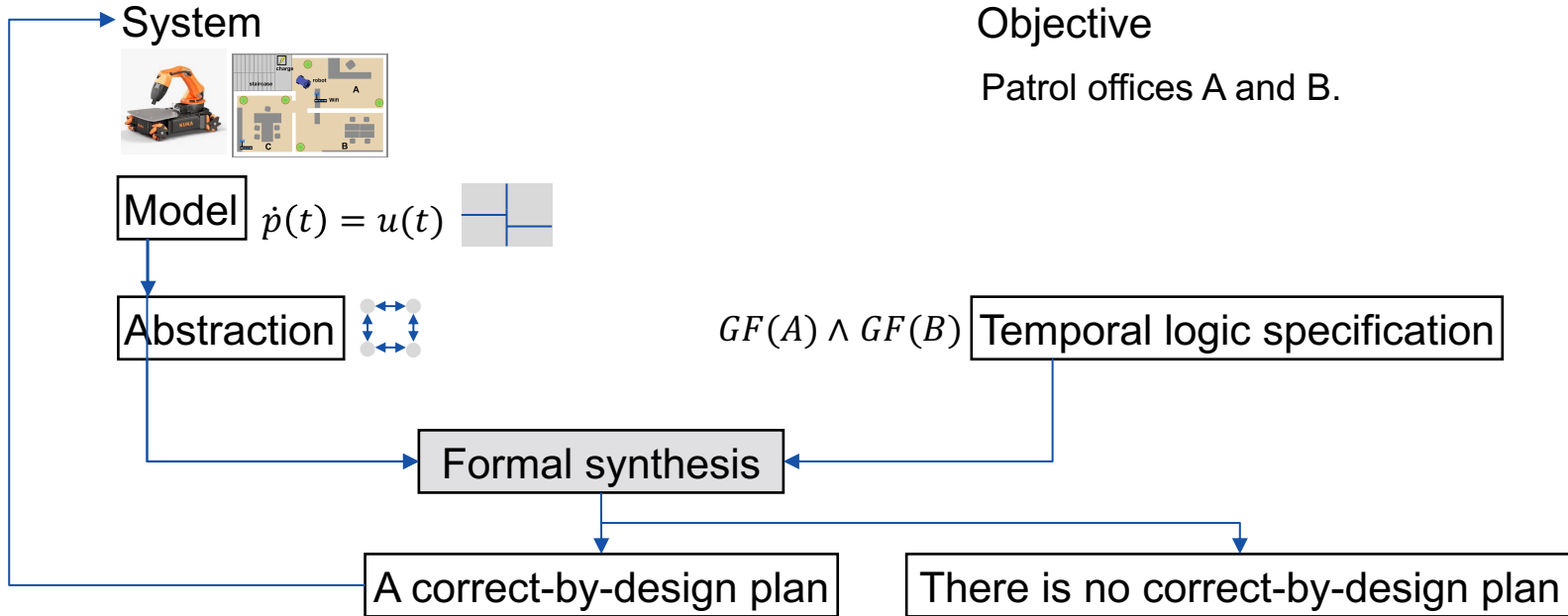
- correct-by-design plan



How do we ensure that they behave as expected?

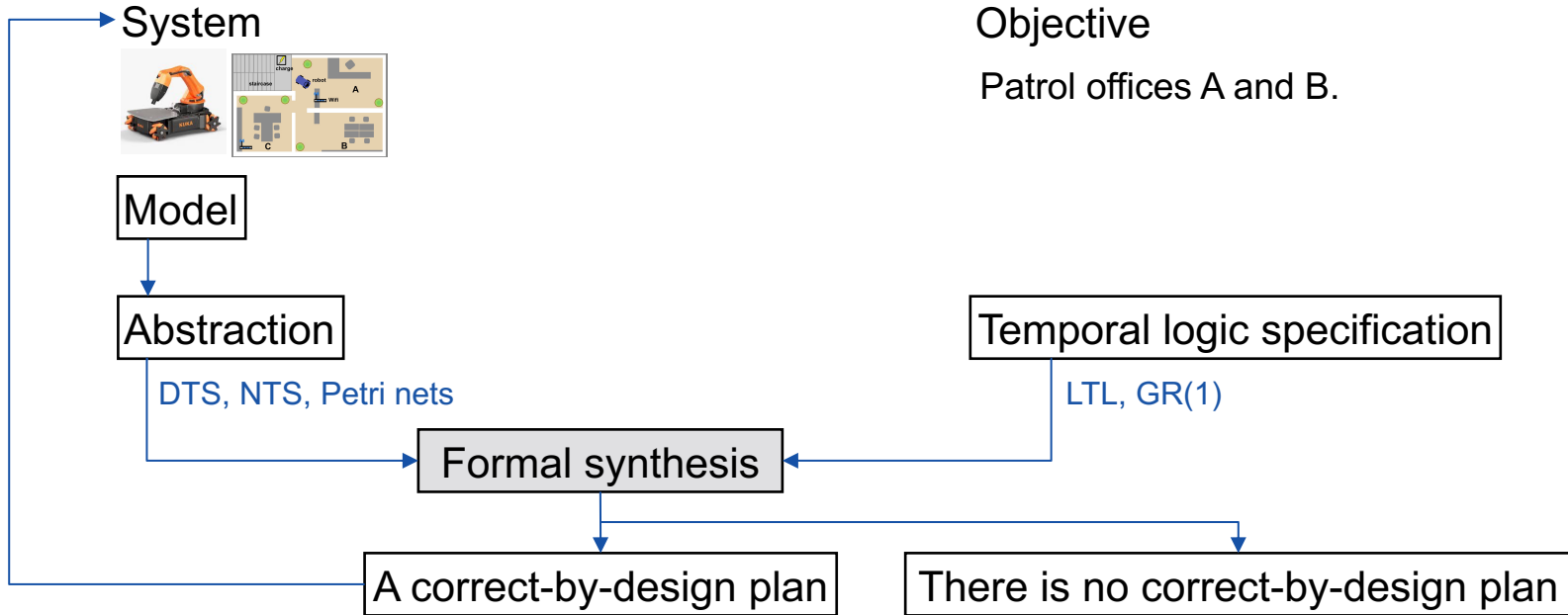


## Formal synthesis





## Formal synthesis (2009)

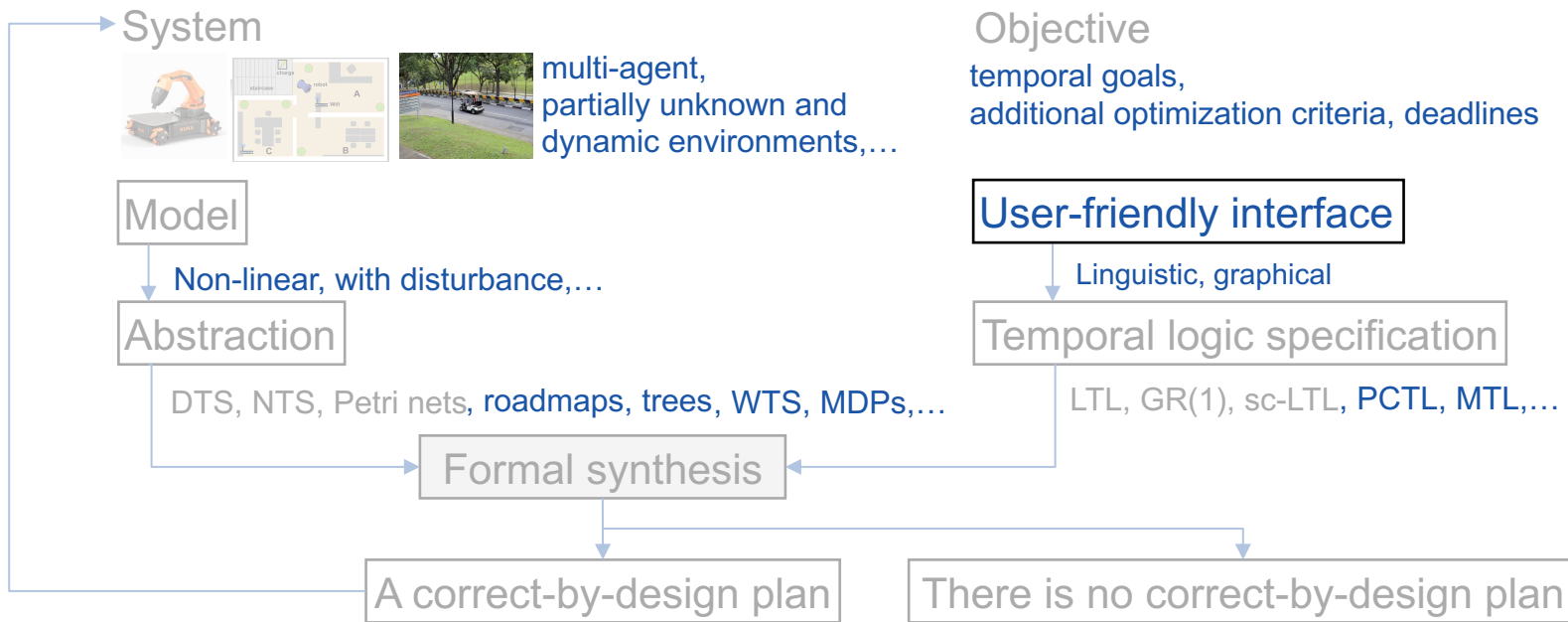


Some seminal works:

[Kress-Gazit et al, TRO 2009, Kloetzer and Belta, TAC 2008]



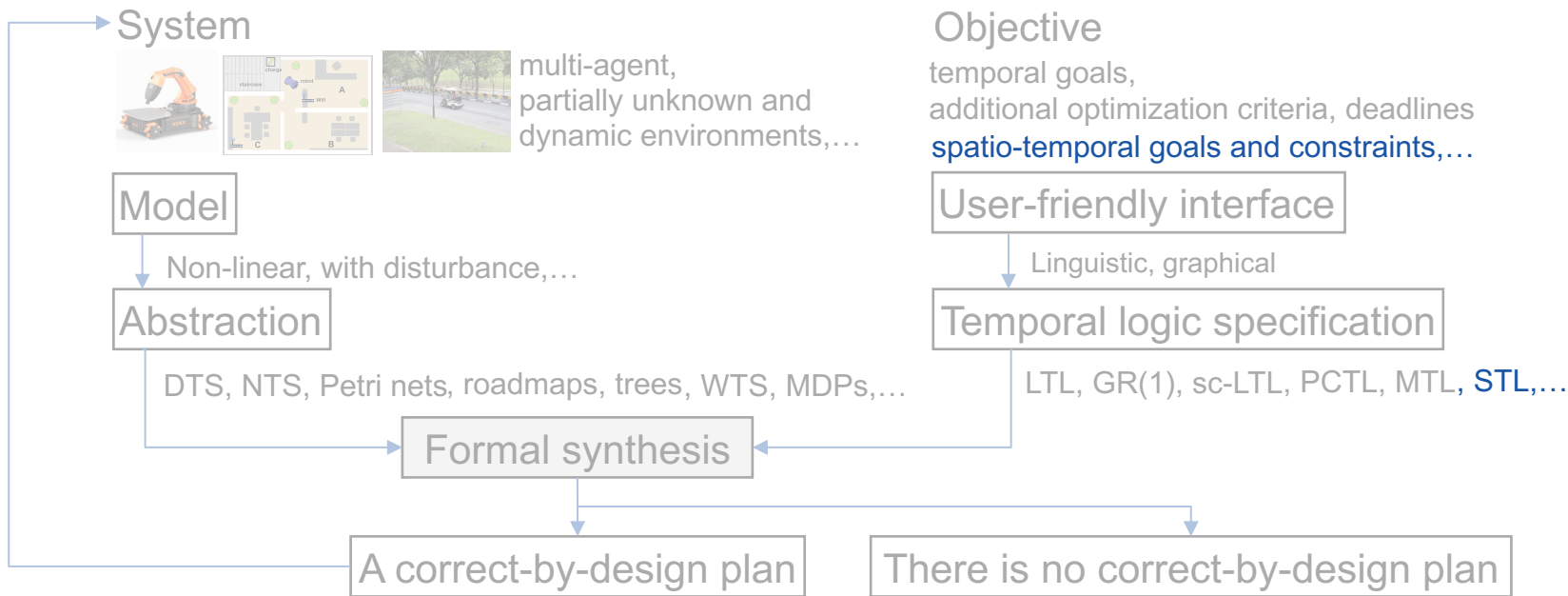
## Formal synthesis (2013)







## Formal synthesis (today)





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## Formal synthesis, integrated



Multi-robot coordination  
for dynamic production assistance



**BOSCH**  
Invented for life



National  
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**PAL**  
ROBOTICS



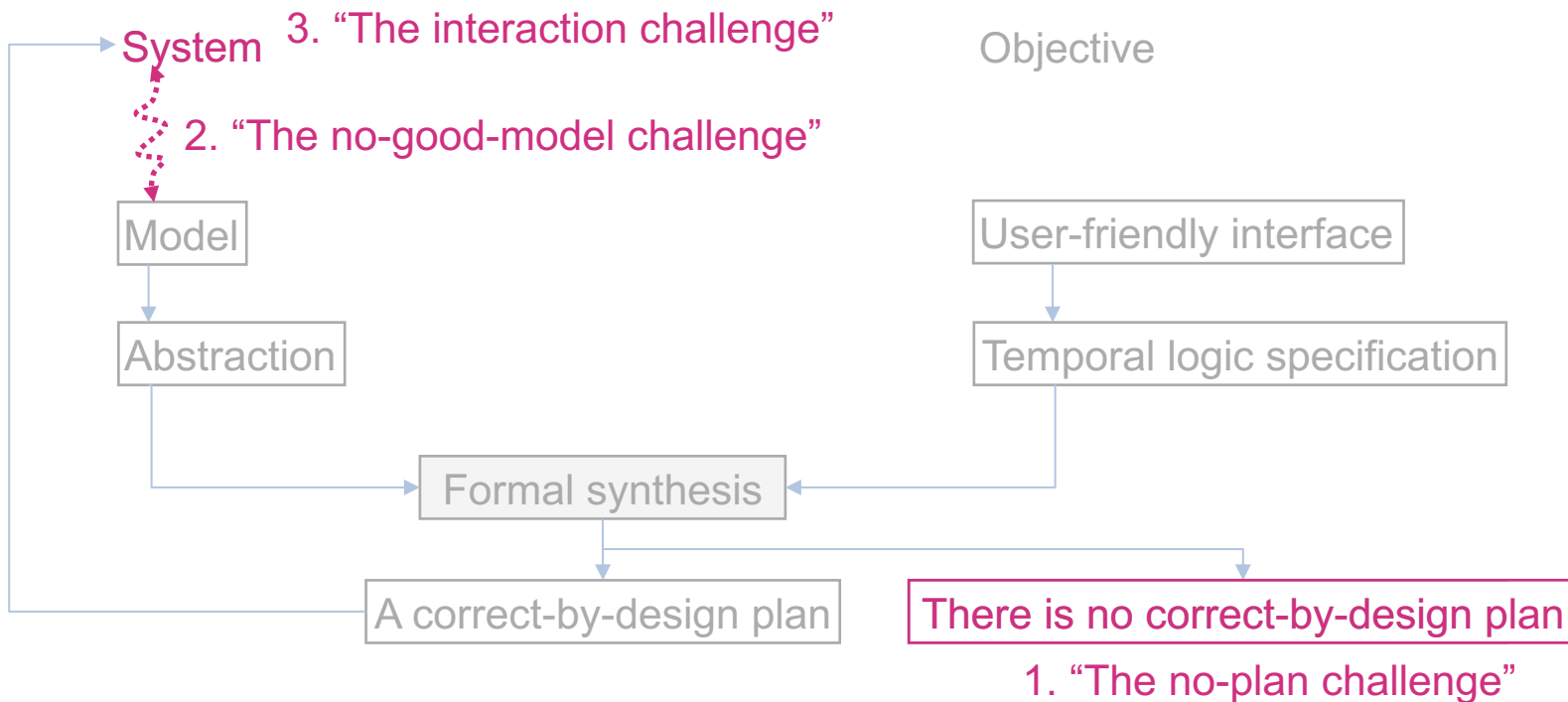
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[www.co4robots.eu](http://www.co4robots.eu)

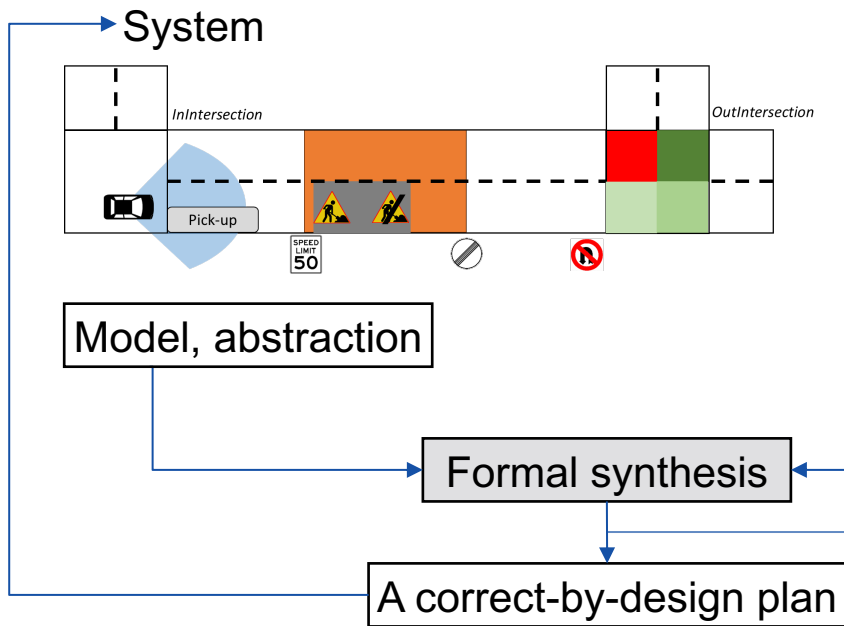


## Three challenges of formal synthesis





# 1. The no-plan challenge



## Objective

Obey the traffic rules:

- Do not cross the full lane
- Stay in the right lane
- Do not enter the construction zone
- Do not enter sidewalk

...

Temporal logic specification

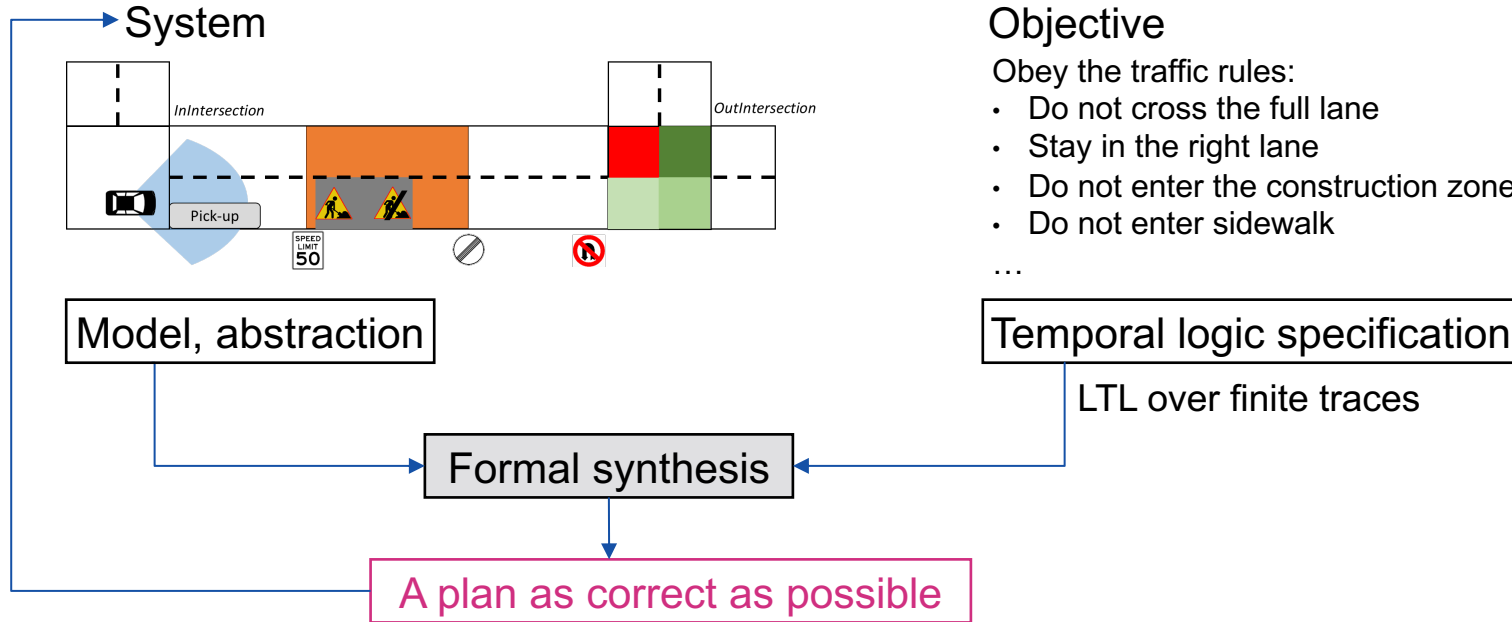
LTL over finite traces

**There is no correct-by-design plan**

All the traffic rules cannot be obeyed simultaneously



## 1. The no-plan challenge



The traffic rules are violated only for the absolutely necessary, for the necessary time



## Quantitative evaluation of LTL

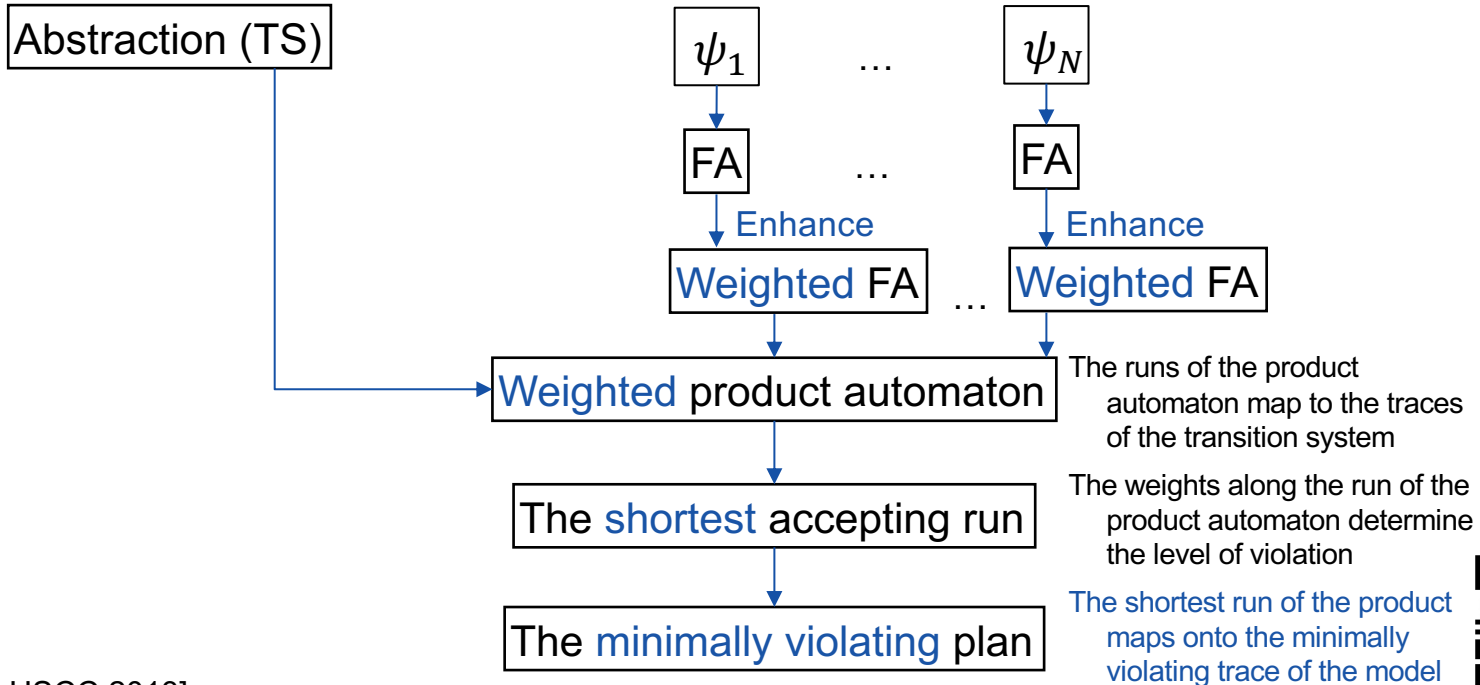
Assume a transition system from RRT\* or other abstraction

**Level of violation**  $\lambda(\text{trace}, \text{LTL formula})$ : the time duration associated with the discrete transitions that need to be removed to make the trace satisfy the LTL formula, weighted by the penalty





## Minimum-violation automata-based FS





## MV-RRT\*

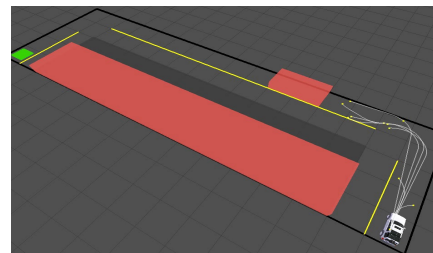
- Incrementally build
- Incrementally update
- Optimality criterion

### RRT\*

- weighted tree
- shortest path
- distance

### MV-RRT\*

- weighted product automaton
- minimally violating path
- primarily level of violation, then distance



[Reyes-Castro et al CDC 2013]

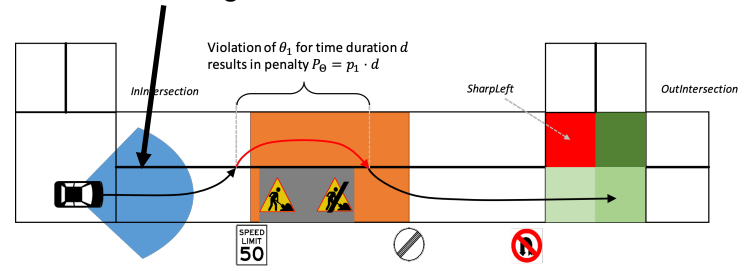




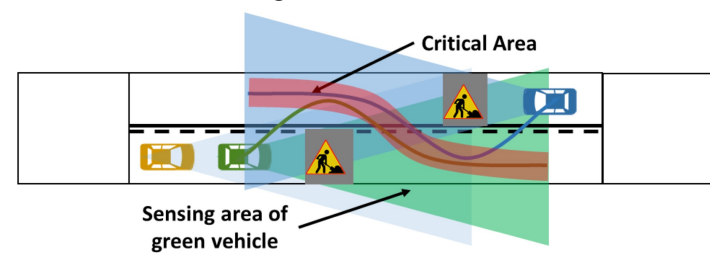
## MV-RRT\* in autonomous driving



Limited sensing:



Multi-vehicle settings:

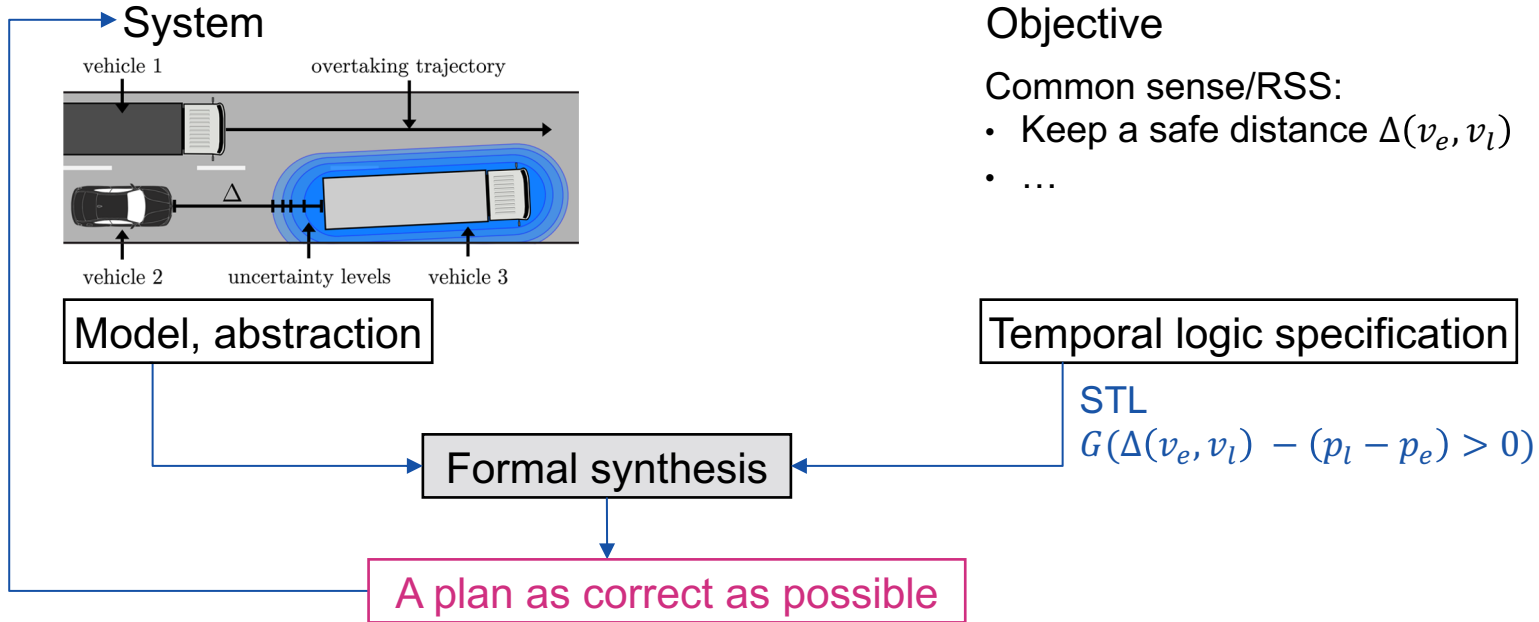


[Reyes-Castro et al HSCC 2013, Vasile et al ICRA 2017, Karlsson et al ICRA 2018, CASE 2020, ICRA 2021]





## The no plan challenge under uncertainty



### Objective

Common sense/RSS:

- Keep a safe distance  $\Delta(v_e, v_l)$
- ...

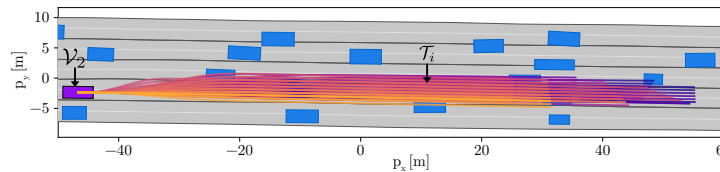
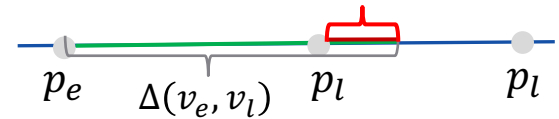
The severity of violation, the probability of violation, and the level of uncertainty are taken into account



## Risk-aware planning in autonomous driving

- Safety specification:  $G(h(x(t)) > 0)$
- Severity function: 
$$l_h(x) = \begin{cases} \ell(h(x(t))), & h(x(t)) > 0 \\ 0, & \text{otherwise} \end{cases}$$
- Severity of violation:  $L = l_h(\hat{x})$
- Risk:  $E[L]$
- Risk-aware planning

$$G(\Delta(v_e, v_l) - (p_l - p_e) > 0)$$



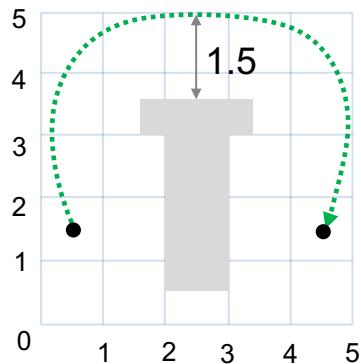
US101 highway scenario



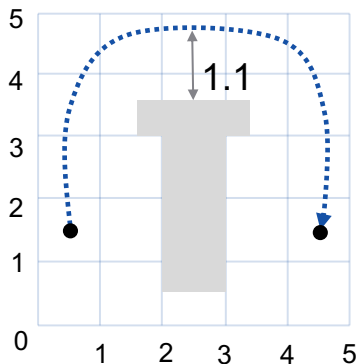


## Signal Temporal Logic spatial robustness

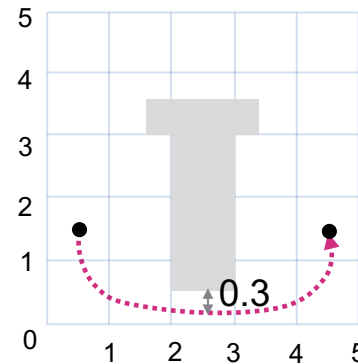
$$G(1 - dist(\sigma, M) > 0)$$



0.5



0.1



-0.7

See [Donze and Maler, LNCS, 2013]



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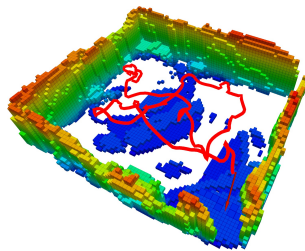
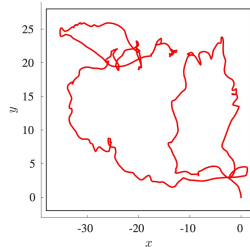
## STL as a preference specification





## STL-guided autonomous exploration

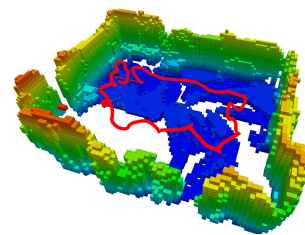
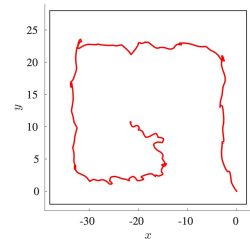
AEP



## Guiding Autonomous Exploration with Signal Temporal Logic

Fernando S. Barbosa, Daniel Duberg, Patric Jensfelt and Jana Tumova

AEP + STL  $G(\text{dist}(\sigma, M) - 1 > 0)$



[Barbosa et al RA-L 2019]





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## 2. The no-good-model challenge

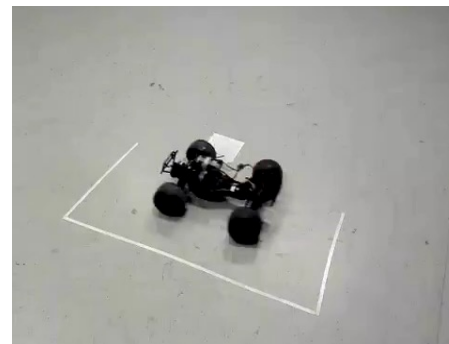
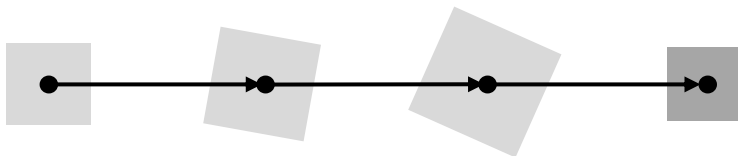




## Safe multi-step feedback motion primitives

for non-holonomic system with bounded disturbance

- Divide the input space into regions & linearize
- Linearization introduces error



- The error can be corrected in  $k$  steps
- The motion primitives can be chained and refined

[Tajvar et al ISSR 2019, CASE 2020, IROS 2021]



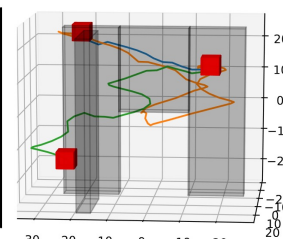
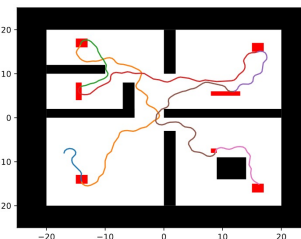
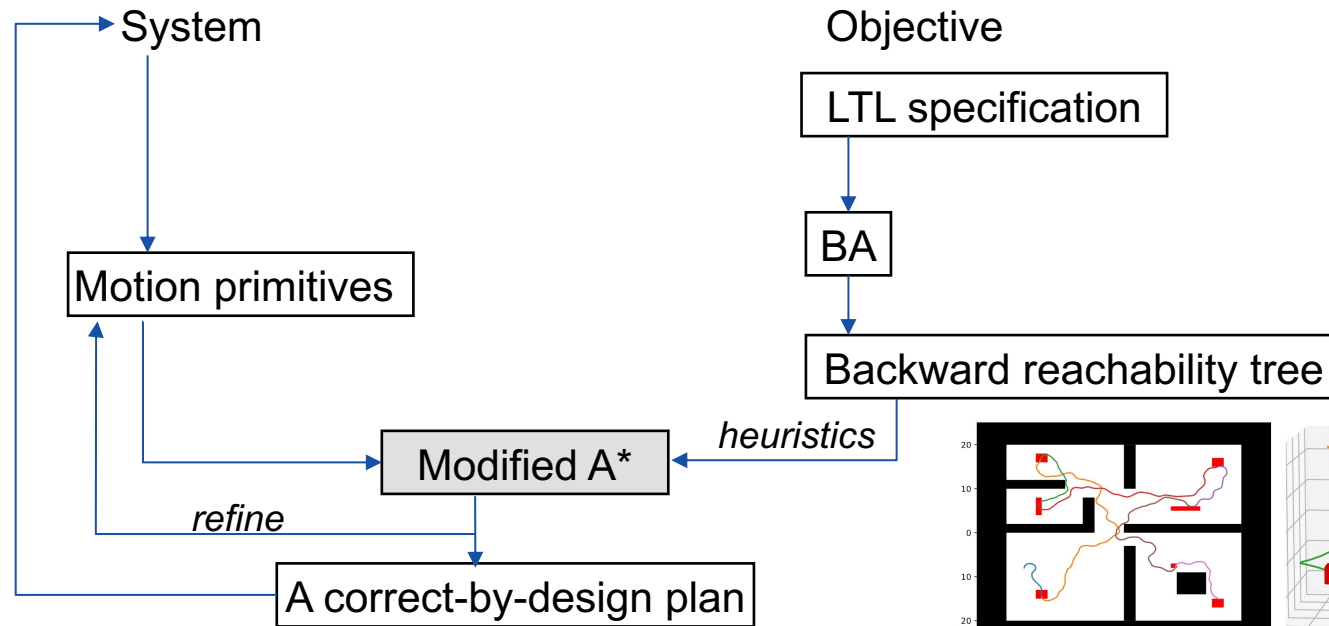




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## LTL planning with motion primitives



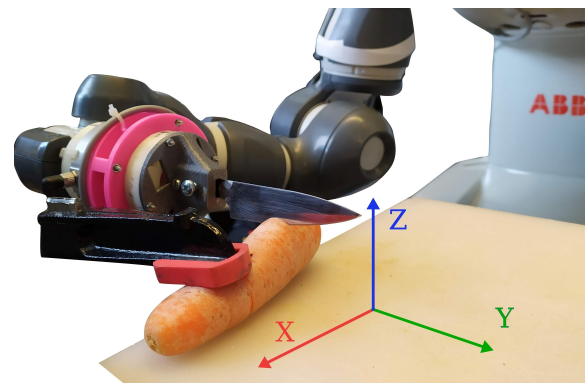
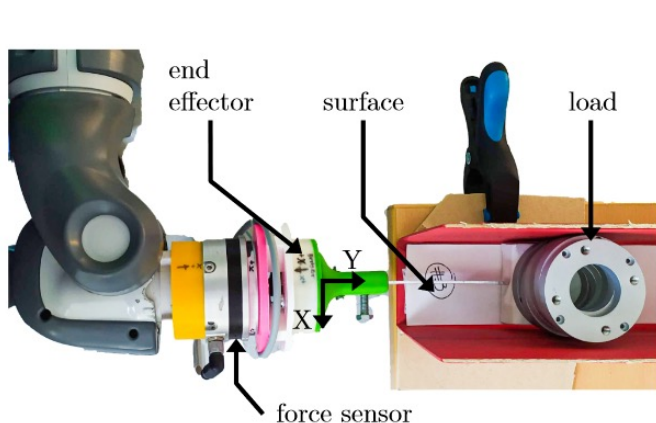
[Tajvar et al CASE 2020]



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## Towards safe data-driven contact-rich manipulation



[Mitsioni et al Humanoids 2021]





## The ~~inter~~ interaction challenge

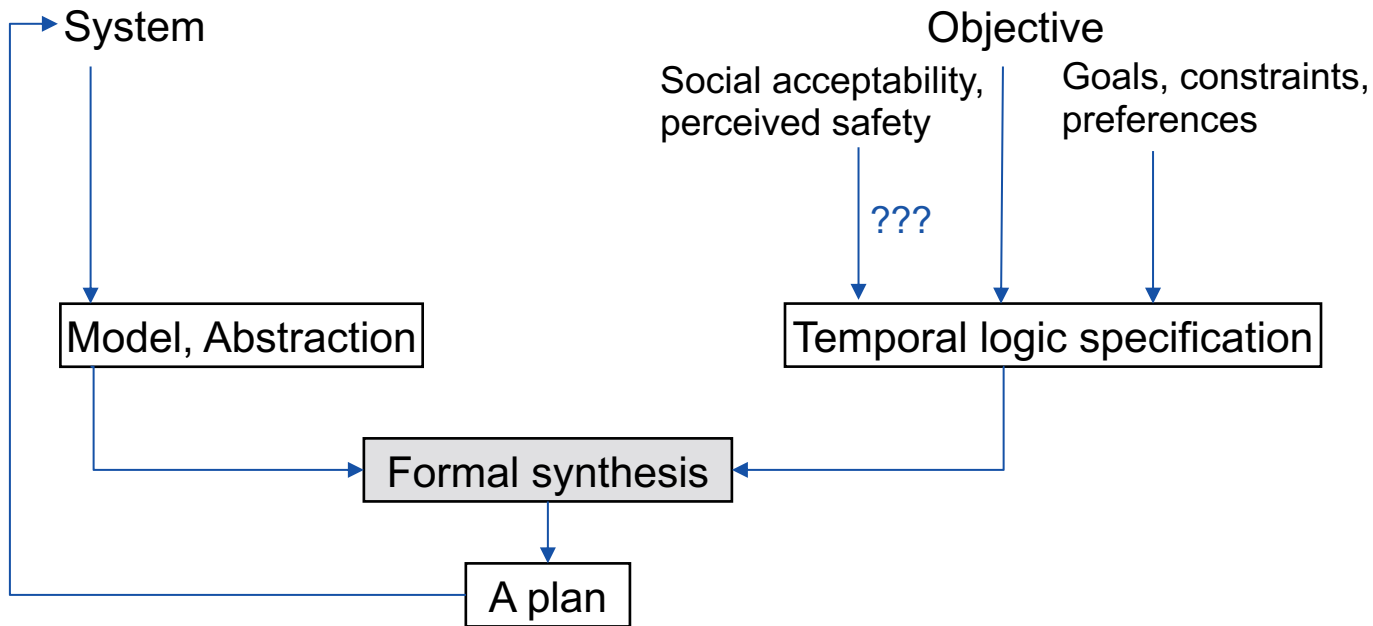




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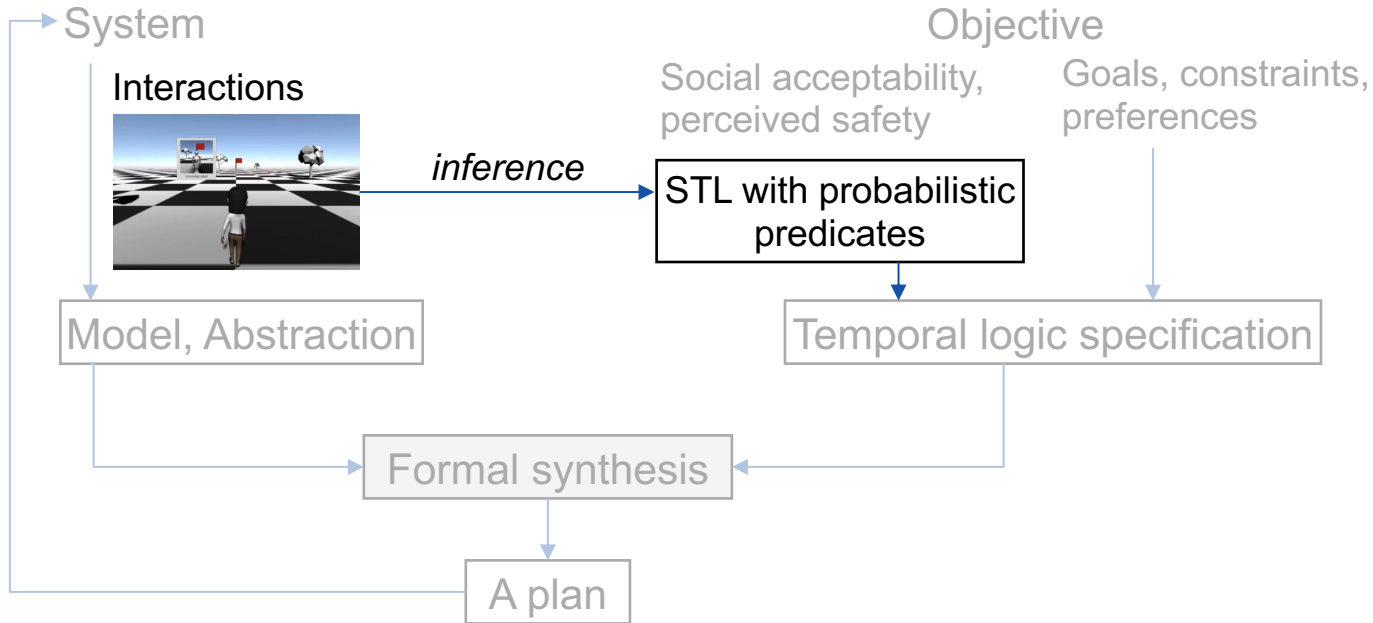


## Correct-by-design and socially acceptable plan





## Correct-by-design and socially acceptable plan





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## I wish I had time to talk also about

- Provable safety vs. perceived safety
- Assumption-guarantee synthesis



- Decentralized multi-agent coordination with temporal logic specifications



## Take-aways

- Temporal logics and formal synthesis to address
  - How do we tell robots what to do?
  - How do we ensure that they behave as expected?
- Rigorous, **but not rigid**:
  - Can be used to provide guarantees if that is desired and possible
  - No need to freeze if a correct-by-design plan does not exist
  - Support for preferences, not just mission/safety-critical goals



## The future: Moving forward to the wild

- Well-defined mathematical objectives → “Soft” objectives
- Guarantees → Risk-awareness
- Manually created models and specifications → Data-driven models and specifications
- FS or learning → FS and learning  
RL with TL goals, RL with TL constraints,
- Component-view → System-view





# Thanks!



Pouria Tajvar, Truls Nyberg, Fernando Barbosa, Wei Wang, Albin Larsson Forsberg, Georg Schuppe, Alexis Linard, Christian Pek, Jesper Karlsson



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